







AddMore Federation

Calculation Policy







The AddMore Fedaeration are passionate about Maths! As Maths is a core subject, it is taught daily - both in discrete lessons and, whenever possible, incorporated into other areas of the curriculum. The purpose of teaching in Mathematics is to ensure our children develop an ability to solve problems, to reason, to think logically and to work systematically and accurately.

We believe that all our children are challenged and encouraged not only to meet the expectations of the National Curriculum, but to also excel in Maths and enjoy the journey that it takes them on! We have adopted the White Rose Mixed Age schemes of work, to allow us to teach maths at the appropriate levels across our mixed aged classes. New mathematical concepts are introduced using a 'Concrete, Pictorial and Abstract' (CPA) approach, this enables all children to experience practical hands-on learning when discovering new mathematical topics, allowing children of all learning styles to access and enjoy maths. This method also allows our children to have clear models and images to aid their understanding, which they will then take with them throughout their mathematical journeys.

"The essence of mathematics is not to make simple things complicated, but to make complicated things simple."

Stan Gudder







Addition and Subtraction







Nursery: 22-36 months

Selects a small number of objects from a group when asked, for example, 'please give me one', 'please give me two'.

Creates and experiments with symbols and marks representing ideas of number

Begins to make comparisons between quantities.

Uses some language of quantities, such as 'more' and 'a lot'

Knows that a group of things changes in quantity when something is added or taken away.

Representations	Key knowledge and vocabulary	Concrete & pictorial Conceptual modelling	Abstract Skills and knowledge	Application across the environment
	Concepts of quantity, equality and inequality. Modelling combining sets of small quantities.	Natural materials and physical objects in all environments. Pictures to show one or two items. Objects and resources to physically represent a quantity. Images and	Spoken number names. One, once, alone, first.	Wonderful one and terrific two displays. Hiding objects find one of, or lots of in the sand, across the setting.
Che is smaller than	Modelling adding to a quantity to make it bigger. Removing objects from a set to show the amount is now smaller.	pictures to represent a small quantity. Using dishes/hoops to make quantities of different values that visually show one set has more than the other.	Mark making and graphics to represent a small number in the context of play.	Matching one item to another then to one image. Repeat with two. Snack time: one piece of fruit to one person, two pieces each
		Images of quantities to compare. Which has more?	Mark making and graphics to represent a small quantity to compare in the context of play.	Problem solving: "We need one/two each how can we sort the bears?"



Nursery/Reception: 30 - 50 months





Knows that numbers identify how many objects are in a set. Beginning to represent numbers using fingers, marks on paper or pictures. Sometimes matches numeral and quantity correctly. Compares two groups of objects, saying when they have the same number. Separates a group of three or four objects in different ways, beginning to recognise that the total is still the same. Shows an interest in representing numbers. Key Vocabulary Concrete & pictorial Abstract Application across the Key knowledge Representations Skills and knowledge environment Conceptual modelling Concepts of cardinality, Layers of vocabulary Natural materials and Represent a quantity by Construction. What can you make with equality, inequality and physical objects in all drawing. rearranging the same environments to count. 3/4 bricks? quantity. (cardinality) Pictures to show a Mark making and Small world. Appendix Counting to 3. One to quantity that can be graphics to represent a Put three carriages on Beck's Tiers of Inequality: bigger, smaller, more one correspondence. small quantity and the train. counted. Vocabulary one in smaller than **Build models** Knowing how many are How many cars are in the attempts at numerals. two. Two is smaller than in the set. Two is more Use fingers to show small car park? than one. Three is more amounts. **Basic to subject specific** Comparing numbers 1,2 than two. Images and pictures to Mark making and Three is more and 3 – 'bigger' and (Beck's Tiers): han one* represent a small drawings to replicate the How many skittles have 'smaller' Add, more, and, make, concrete and pictorial you knocked over? quantity. sum, total, altogether, Stable ordering numbers model. Mark making and double, how many 1 to 3. Resources that match a graphics to represent a 3 is made up of 2 and 1. numeral to a quantity. small number in the Instructional vocabulary: E.g. a number track, context of play. Listen, join in, say, start Using counting strategies digits cards with With models, attempts from, look at, carry on and subitising to identify numerals and quantities to write numerals and the number of concrete represented. continue to mark make. objects in the set.







Reception: 40 - 60 months

Counts up to three or four objects by saying one number name for each item. Counts objects to 10 and beginning to count beyond 10.

Selects the correct numeral to represent 1 to 5, then 1 to 10 objects. Uses the language of 'more' and 'fewer' to compare two sets of objects. Finds the total number of items in two groups by counting all of them. Says the number that is one more than a given number.

In practical activities and discussion, beginning to use the vocabulary involved in adding and subtracting.

	Key Vocabulary	Key knowledge and vocabulary	Concrete & pictorial Conceptual modelling	Abstract	Application across the environment
Representations		,		Skills and knowledge	
	Layers of vocabulary	Number structure. Equality,	Natural materials, physical	Represent a quantity by	Malleable play: problem solving 'Let's
		inequality. Partitioning and	objects and mathematical	drawing or by using	put 5 cherries on the cakes.'
	Appendix Beck's Tiers of Vocabulary	recombing. Subitising to 5. 5 as an anchor. Modelling the combining of sets, recognising that the	resources e.g. counters in all environments to count accurately. (cardinality). To 10 and beyond. Pictures to show a quantity that can be counted then to 10 and beyond.	graphics. (using drawings to show a resource) Mark making and graphics to represent numbers to 10 and beyond in their play.	'How will you put your 5 candles on the two cakes?' Role play: problem solving Each shelf in the shop must have 5 or more items to sell.
		quantity has increased.			How shall we arrange the items?
	Basic to subject specific (Beck's Tiers):	Using counting strategies and	Resources that match a numeral to a quantity	Graphics and attempts at numerals in the correct orientation.	Find items in the sand.
	Add, more, and, make, sum, total, altogether, double, how many more to make, how	nake, ther, y w	Models of mathematical counting resources to show the more or fewer. Using a		altogether?







many are left, how	number track or line to	Mark making and numerals
many have gone?	show one more than a given	to replicate the concrete
Instructional	number	and pictorial model.
vocabulary: Listen, join		Graphics and numerals to
in, say, start from, look		show the addition
at, carry on, what		
comes next, find,		
choose, talk about		







Reception: ELG 2018

Numbers to 20: place them in order and say which number is one more or one less than a given number Using quantities and objects, they add and subtract two single-digit numbers and count on or back to find the answer They solve problems, including doubling, halving and sharing.

They solve problems, including doubling, having and sharing.						
Representations	Key Vocabulary	Key knowledge and vocabulary	Concrete & pictorial Conceptual modelling	Abstract Skills and knowledge	Application across the environment	
3 + = 6 1 + 5 = = + 0 = 6 3 + 3 = = 5 + = 6	Layers of vocabulary Appendix Beck's Tiers of Vocabulary Basic to subject specific (Beck's Tiers): Add, more, and, make, sum, total, altogether, double, how many more to	Number structure. Equality, inequality. Partitioning and recombing. Subitising to 5. 5 as an anchor. Modelling the combining of sets, recognising that the quantity has increased. Using counting strategies and subitising to identify the number of	Natural materials, physical objects and mathematical resources e.g. counters in all environments to count accurately. (cardinality). To 10 and beyond. Pictures to show a quantity that can be counted then to 10 and beyond. Resources that match a numeral to a quantity	Represent a quantity by drawing or by using graphics. (using drawings to show a resource) Mark making and graphics to represent numbers to 10 and beyond in their play. Graphics and attempts at numerals in the correct orientation. Mark making and numerals to replicate the	Malleable play: problem solving 'Let's put 5 cherries on the cakes.' 'How will you put your 5 candles on the two cakes?' Role play: problem solving Each shelf in the shop must have 5 or more items to sell. How shall we arrange the items? Find items in the sand. 3 shells and 2 fish. How many items altogether?	







$ \begin{array}{c} 6 = 6 + \\ 6 = + 5 \\ 6 = 2 + \\ 6 = + 3 \\ 6 = + 3 \\ 6 = + + + 3 \end{array} $	make, how many are left, how many have gone? One less, two less, ten less, the difference between, odd and even. Instructional vocabulary: Listen, join in, say, start from, look at, carry on, what comes next, find, chose, talk about, repeat, tell me, describe, complete	concrete/pictorial objects in the set	Models of mathematical counting resources to show the more or fewer. Using a number track or line to show one more than a given number	concrete and pictorial model. Graphics and numerals to show the addition		
	Reception: ELG 2018 Numbers to 20: place them in order and say which number is one more or one less than a given number Using quantities and objects, they add and subtract two single-digit numbers and count on or back to find the answer They solve problems, including doubling, halving and sharing.					
Representations	Key Vocabulary	Key knowledge	Concrete & pictorial Conceptual modelling	Abstract Skills and knowledge	Application across the environment	
Counting in 2s	Layers of vocabulary Appendix Beck's Tiers of Vocabulary	Knowing that groups of the same quantity are added together. That is what makes a double. The quantity divided into two equal groups. Halving.	Natural materials, physical objects and mathematical resources e.g. counters in all environments to double, share, group and half accurately.	Represent a quantity by drawing or by using graphics. (using drawings to show a resource) Graphics and numerals to show the double/halving/grouping and sharing used.	In small world play: All the animals in the enclosures are doubles. How many lions will there be etc? Doubles shop Everything in the shop has to be double.	







		Sharing and grouping.	Modelling and	
Counting in 5s	Basic to subject		demonstrating groups of	Snack time
	specific (Beck's	Sharing is where you take	and shared quantities.	How will we share the fruit so that
	Tiers):	a quantity and count out		we can have half each?
00 00	Add, more, and,	into how many equal	Showing that the quantity	
	make, sum, total,	groups you want.	has increased when	
	altogether, double,		doubled and reduced	
00 00	how many more to	Grouping is where you	when halved.	
	make, how many	take the quantity and		
Double 10 is 20.	are left, how many	make the groups (of two,		
	have gone?	or three etc)		
	One less, two less,			
	ten less, the			
	difference between,			
	odd and even.			
	Equals, share,			
8 divided in to groups of 2.	groups of, halve and			
	half			
1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1				
	Instructional			
	vocabulary:			
	Listen, join in, say,			
	start from, look at,			
	carry on, what			
4 shared equally into two groups.	comes next, find,			
	choose, talk about,			
	repeat, tell me,			
	describe, complete,			
	pattern, remember,			
	ring, work out,			
	check, another way			







To halve the apple it would be cut into two equal pieces			
To halve the satsuma we would count the segments and share them equally.			
Double the number of ladybirds. This show half the number of lady birds sitting on the leaf.			
Doubling and halving.			







Addition- KS1

EYFS	 Reception: ELG 2020 Have an understanding of number to 10, linking names of numbers, numerals, their value, and their position in the counting order. Subitise (recognise quantities without counting) up to 5. Automatically recall number bonds for numbers 0-5 and <i>for 10</i>, including corresponding partitioning facts. Automatically recall double facts up 5+5 Compare sets of objects up to 10 in different contexts, considering size and difference Explore patterns of numbers within numbers up to 10, including evens and odds. 				
Year	1	2			
Layers of vocabulary Appendix Beck's Tiers of Vocabulary	 Basic to subject specific (Beck's Tiers): +, add, more plus make, sum, total altogether score double, near double one more, two more ten more how many more to make? how many more is than? how much more is? Instructional vocabulary: start from, start with, start at look at point, to show me 	 Basic to subject specific (Beck's Tiers): +, add, addition, more, plus make, sum, total altogether score double, near double one more, two more ten more one hundred more how many more to make? how many more is than? how much more is? Instructional vocabulary: tell me, describe, name, pick out, discuss, talk about, explain, explain your method, explain how you got your answer, give an example of show how you 			
NC 2014	Read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs.	Using concrete objects and pictorial representations, including those involving numbers, quantities and measures applying their increasing knowledge of mental and written methods			
	Concrete, pictorial, abstract	Concrete, pictorial, abstract			















Addition- KS2

KS1	Pupils should practise addition to 20 and within to become increasingly fluent. They should use the facts they know to derive others, e.g using 7 + 3 = 10 to find 17 + 3 = 20, 70 + 30 = 100They should use concrete objects and practical apparatus, such as bead strings and number lines to explore additions including missing numbers. Use pictorial representations such as bar models and whole part diagrams to show additive relationships. 100 squares could be used to explore patterns in calculations such as 74 +11, 77 + 9 encouraging children to think about 'What do you notice?' where partitioning or adjusting is used.Pupils should learn to check their calculations, by using the inverse. They should continue to see addition as both combining groups and counting on. They should use Dienes to model partitioning into tens and ones* and learn to rearrange numbers in different ways e.g. 23 = 20 + 3 = 10 + 13.					
	Show understanding tha	t adding zero leaves a nu	mber unchanged.			
Year		3			4	
Layers of vocabulary Appendix Beck's Tiers of Vocabulary	Basic to subject specific (Beck's Tiers): +, add, addition, more, plus make, sum, total altogether score double, near double one more, two more ten more one hundred more how many more to make? how many more is than? how much more is? Instructional vocabulary: explain your method explain how you got your answer give an example of show how you show your working			 Basic to subject specific (Beck's Tiers): add, addition, more, plus, increase sum, total, altogether score double, near double how many more to make? Instructional vocabulary: calculate, work out, solve investigate, question answer check 		
NC 2014	Add and subtract numbers with up to 3 digits, using formal written methods of columnar addition and subtraction.			Add and subtract numbers with up to 4 digits using the formal written method of columnar addition and subtraction where appropriate. Solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why.		
Developing Conceptual/ Procedural Understanding	Near doubles 13+14 = Double 13= 26 26+1 =27	Start with least significant digit	Columnar addition	Using known facts 40 + 80 = 120 using 4 + 8 = 12	Columnar addition	Columnar addition (decimals) in contexts such as money and measurement







or	67	625	So 400 + 800 = 1200 and	587	12.45
Double 14 =28	+ 24	+ 48	4000+8000=12.000	+ 475	7.36
28-1=27	11 (7+4)	673		1062	<u>+ 24.50</u>
Using known facts	+ 80 (60+20)	1		11	44.31
40 + 80 = 120 using 4 +	91			"7 add 5 equals 12.	1 1 1
8 = 12	-	Teach the carried	Remodelling strategy	That's 2 units and 1	
So 400 + 800 = 1200	"7 add 4 equals 11	digit.	3548 + 1998	ten to carry over. 80	Representing problems
	and 60 add 20 equals		3546 + 2000 = 5546	add 70 equals 150	There are 259 more boys than girls in
	80. 1+ 0 = 1 and 1 ten			and the1 ten to carry	Lucy's school. If there are 789 girls,
	+ 8 tens = 9 tens"		Place value materials to	makes 160. That's 6	how many pupils are there altogether?
			represent calculations	tens and 100 to carry	
Remodelling strategy				over. 500 add 400	2
243 + 198				equals 900 and the 1	·
241 + 200 = 441				hundred to carry	759 759 + 259
				makes 1000"	
Place value materials	III	Representing			
to represent 3 digit		problems		7648	
numbers		There are 334		<u>+1486</u>	
Base 10 and then place	625	children at		14 (8+6)	
value counters.	<u>+ 48</u>	Springfield School		120 (40+80)	
	13 (5+8)	and 75 at Oak		1000 (600+400)	
	60 (20 + 40)	Nursery. How		+ <u>8000 (</u> 7000+1000)	
	+ <u>600</u> (600 + 0)	many children are		<u>9134</u>	
	<u>673</u>	there altogether?			
				7648	
	All language in the			<u>+ 1486</u>	
	context of the place			<u>9134</u>	
10 1	value and the mental			111	
	addition of the totals				
	to be done in any				
	order.				







Year		5	6		
	Basic to subject specific (E	Beck's Tiers):	Basic to subject specific (Beck's Tiers):		
Layers of vocabulary	add, addition, more, plus,	increase sum, total, altogether score double,	add, addition, more, plus, increase sum,	total, altogether score double, near double	
	near double how many m	ore to make?	how many more to make?		
All and a second s	Instructional vocabulary:		Instructional vocabulany:		
122.	nut place arrange rearra	nge change, change over split, separate	nut place arrange rearrange change ch	ange over adjusting adjust split separate	
Appendix	put, place all alige, leal a	nge change, change over spirt, separate	carry on continue repeat what comes n	ext2 predict describe the pattern describe the	
Beck's Tiers of			rule	ext: predict describe the pattern, describe the	
Vocabulary			find find all find different investigate		
NC 2014	Add and subtract whole n	umbers with more than 4 digits, including	Solve problems involving addition, subtraction, multiplication and division.		
	using formal written meth	ods (columnar addition and subtraction).			
	Solve addition and subtrac	ction multi-step problems in contexts,			
	deciding which operations	and methods to use and why.		T	
Developing	Columnar addition	Representing problems	Columnar addition	Representing problems	
Conceptual/	Include calculations	If 2541 is the answer, what's the question?	Include calculations with up to 3	7208 females attended a concert as well as	
Procedural	involving more than 2	 Can you create three addition 	'empty columns'.	8963 males. There were originally 20000	
Understanding	numbers and carrying	calculations? - Can you create three	128.7 + 3.014	seats on sale. How many empty seats were	
	figures >1.	subtraction calculations? - Did you use a		there at the concert?	
		strategy?	128.700		
	25567		+3.014		
	16397		<u>131.714</u>		







+15984 57948 1 1 2 1	1	
Include calculations with 'empty columns'. 124.9 + 7.25		
124.90		
$\frac{+ 7.25}{\underline{132.25}}$		







Subtraction- KS1

EYFS	 Reception: ELG 2020 Have an understanding of number to 10, linking names of numbers, numerals, their value, and their position in the counting order. Subitise (recognise quantities without counting) up to 5. Automatically recall number bonds for numbers 0-5 and <i>for 10</i>, including corresponding partitioning facts. Automatically recall double facts up 5+5 Compare sets of objects up to 10 in different contexts, considering size and difference Explore patterns of numbers within numbers up to 10, including evens and odds. 							
Year	1	2						
Layers of vocabulary Appendix Beck's Tiers of Vocabulary	Basic to subject specific (Beck's Tiers): take away, distance between, difference between, less than. How many more? How much greater? How many fewer? how much more is? – subtract, take (away), minus, leave, how many are left/left over? how many have gone? one less, two less, ten less how many fewer is than? how much less is? difference between half, halve = equals, sign, is the same as Instructional vocabulary: start from, start with, start at look at point, to show me	 Basic to subject specific (Beck's Tiers): subtract, subtraction, take (away), minus leave, how many are left/left over? one less, two less ten less one hundred less how many fewer is than? how much less is? difference between half, halve = equals, sign, is the same as tens boundary difference, partition, rearrange, inverse, place value Instructional vocabulary: tell me, describe, name, pick out, discuss, talk about, explain, explain your method, explain how you got your answer, give an example of show how you 						
NC 2014	Read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs.	Using concrete objects and pictorial representations, including those involving numbers, quantities and measures applying their increasing knowledge of mental and written methods						
	Concrete, pictorial, abstract	Concrete, pictorial, abstract						







Developing Number bonds Count back on a Develop Whole-part model Subtract mentally pairs of Re-arranging Conceptual/ number track. knowledge of fact 35 - 8 = multiples of 10 using known 15 7 77 Tell me what you 15 - 6 = 9families. Procedural facts Astall Hotel 00000 (0) 7×5+1 1+1×1 7-2=1 7×1=1 know about 8, e.g. 2 + Understanding 60 - 20 = 40 because 6 - 2 = 4mommo 6, 5 + 3 Whole-part model Difference between. 35 - 8= 9+7+10 1=9=00 18.) Astall Iviali Partitioning of the second Rearrange the 8 Fill in the missing number strategy 13 - 8 into 5 + 3 numbers = So 35 - 5 - 3= 30 - 3 All answers to be 74 – 47 Ten Frames 8+ = 13 =27 recorded in a number 74 - 40 = 34Subtraction-take 000 sentence following any 34 - 4 - 3 = 2755 - 27 = Difference between 7 and 10. 000 awav P. . . . informal recording. Partition the 27 10 10 - 🗆 = 3 10 - [] = 9 10 - 0 = [] into 20 +7 and Balance in the equation 5 + = 10 +4 = 10rearrange the 7 into 5 + 35 -Adjustment strategy = 31 4.144 2. Use the pattern to complete - 12 =34 77 - 9 = henry's calors So 55 – 27 = 55 - 20 the number sentences. 77-10 +1 =67+ 1 20 -= 14 - 3 -5 -2 12 Fill in the missing =68 (Open-ended) Cakes esters 11111111111 1 4 4. 4. Daloes left. = 35 - 5 numbers = 15 -18 -10 8-3=? - 2 1 1 211111111111 1 1 1 Subtraction-finding = 28 00000 00000 **Decision making** Taking away and the difference (Round and adjust) 6 less than 10 is 4. 27 -= 12 exchanging Feter 中國國際國際國際國際 What is the nearest 10? Count out, then count how Sam works out 73 – 46 = 55 – 27 = many are left. Remove from lanay @@@ ---27 - 15 = 12. 55 - 30 +3 =25 + 3 the set. How many more How could he have done this? = 28 7 - 4 = 3cakes does Peter 91 - 48 =have than Jenny? What do we know 91-50 +2=41 +2 Exchange to make 8-3=? =43 about 76? '60 and 13'. 73 - 46 = 27 Now take away the 46.







Subtraction- KS2

KS1	Pupils should practise subtraction to 20 and within to become increasingly fluent. They should use the facts they know to derive others, e.g using 10 - 7 = 3 and 7 = 10 - 3 to calculate 100 - 70 = 30 and 70 = 100 - 30. Know the effect of zero. As well as number lines, 100 squares could be used to model calculations such as 74 – 11, 77 – 9 or 36 – 14, where partitioning or adjusting are used. Pupils should learn to check their calculations, including by adding to check. They should continue to see subtraction as both take away and finding the difference and should find a small difference by counting up. They should use Dienes to model partitioning into tens and ones* and learn to partition numbers in different ways e.g. 23 = 20 + 3 = 10 + 13.						
Year		3			4		
Layers of vocabulary Appendix Beck's Tiers of Vocabulary	Basic to subject specific (Beck's Tiers): subtract, subtraction, take (away), minus leave, how many are left/left over? one less, two less ten less one hundred less how many fewer is than? how much less is? difference between half, halve = equals, sign, is the same as tens boundary, hundreds boundary exchange, carried digits Instructional vocabulary: explain your method explain how you got your answer give an example of show how you show your working			subtract, subtraction, take (away), minus, decrease leave, how many are left/left over? difference between half, halve how many more/fewer is than? how much more/less is? equals, sign, is the same as tens boundary, hundreds boundary, inverse exchange, carried digits Instructional vocabulary: calculate, work out, solve investigate, question answer check			
NC 2014	Add and subtract numbe	rs with up to 3 digits, usi	ng formal written	Add and subtract numbers	with up to 4 digits using	the formal written method of columnar	
	methods of columnar addition and subtraction. Least significant digit is always dealt with first to establish if the exchange is needed.			addition and subtraction w problems in contexts, deci	where appropriate. Solve ding which operations an	addition and subtraction two-step d methods to use and why.	
Developing	Subtract mentally	Start with least	Columnar	Subtract mentally pairs	Columnar	Representing problems	
Conceptual/	pairs of multiples of	significant digit –	subtraction	of multiples of 1000	subtraction	Check the answer to the following	
Procedural	100 using known facts	decomposition	X B 4	using known facts	2344 -187	calculations using the inverse. Show all	
Understanding	600 - 200 = 400		- 286 468	6000 – 2000= 4000	2 ¹ 31 2344	your working.	
	because 6 – 2 = 4		Emphasis on	because $6-2=4$	- <u>187</u> 2157		
			language of place				







Remodelling strategy (keeping the difference the same) 502 – 198 504 – 200 = 304 Re-arranging Use of apparatus to understand rearrangements, e.g. 55	81 = 80 1 - 57 50 7 	value, i.e. 14 units subtract 6 units, 14 tens subtract 8 tens, and 6 hundreds subtract 2 hundreds.	Remodelling strategy (keeping the difference the same) 3548 - 1998 3550 - 2000 = 1550 Find the difference strategy 13 .6 - 2.8 = +02 +106	6467 – 2684 5131 6467 - 2684 3783 Columnar subtraction (decimals) in contexts such as money and	An intervent a contrast planois on a vieweng montp to triany There may be constant in an So as the first contrast as it is The may be constant in an So as the first contrast as it is The may be constant in an intervent The may be constant in an intervent The may be constant in a intervent The
as 40 and 15(not as part of calculations). Place value materials to represent numbers in calculations	I will rearrange 81 into 70 and 11. 11 subtract 7 equals 4 and 70 subtract 50 equals 20. 20 and 4 make 24." 754 700 50 4 - 86 80 6	Representing problems There are 386 pupils at Oak Primary. If 79 pupils have sandwiches, how many have dinners?	28 3 136 13.6 - 2.8 = 10.8 Place value materials to represent calculations.	measurement 32.34 – 14.18 ^{2.1.2.1} ,32,34 <u>-14.18</u> 18.16	2456- 734 = 1822
100 10 1 100 10 1		386 ? 79			
	o "It's tricky to take 6 from 4 and 80 from 50. I need to rearrange the number. I will exchange one ten from 50 which leaves				







4	0 and makes 14 in the		
u	inits.		
4	0 to subtract 80 is		
tr	ricky. I will exchange		
0	one hundred from 700		
a	ind make 140.		
1	4 subtract 6 equals		
8	3. 140 subtract 80		
e	equals 60 and 600		
SI	ubtract 0 equals 600."		







Year		5		6		
Layers of vocabulary Appendix Beck's Tiers of Vocabulary	Basic to subject specific (I subtract, subtraction, take over? ten less one hund much less is? difference same as tens boundary, h units boundary, tenths bo exchange, carried digits Instructional vocabulary: put, place arrange, rearra split, separate	Beck's Tiers): e (away), minus, leave, how many are left/left red less how many fewer is than? how between half, halve = equals, sign, is the undreds boundary, inverse, undary	 subtract to subject specific (beck's field). subtract, subtraction, take (away), minus, decrease leave, how many are left/left over? difference between half, halve how many more/fewer is than? how much more/less is? equals, sign, is the same as tens boundary, hundreds boundary, units boundary, tenths boundary, inverse Instructional vocabulary: put, place arrange, rearrange change, change over adjusting, adjust split, separate carry on, continue, repeat what comes next? predict describe the pattern, describe the rule find, find all, find different investigate 			
NC 2014	Add and subtract whole n using formal written meth Solve addition and subtra deciding which operation	umbers with more than 4 digits, including nods (columnar addition and subtraction). ction multi-step problems in contexts, s and methods to use and why.	Solve problems involving addition, subtraction, multiplication and division.			
Developing Conceptual/ Procedural Understanding	Columnar subtraction 523/4 $-\frac{1187}{51157}$ Include calculations with 'empty columns'. 324.9 - 7.25 1181 324.90 -7.25 317.65	Representing problemsKangchenjunga is the third highestmountain in the world at 28,169 feet abovesea level. Lhotse is the fourth highest at27,960 feet above sea level. Find thedifference in heights mentally.Keeping the difference, the same to makethe numbers easier to calculate with.	Columnar subtraction Include calculations with up to 3 'empty columns'. 128.7 - 3.014 6 ⁹ 11 128.700 - 3.014 125.686	Representing problems Katie was given the calculation below 47326 – 1900 = She said "I will just take off 2000 then subtract another 100 so my answer is 45126." Is she correct? Would you use her method? Explain your answer		















Part-Whole Model



Benefits

This part-whole model supports children in their understanding of aggregation and partitioning. Due to its shape, it can be referred to as a cherry part-whole model.

When the parts are complete and the whole is empty, children use aggregation to add the parts together to find the total.

When the whole is complete and at least one of the parts is empty, children use partitioning (a form of subtraction) to find the missing part.

Part-whole models can be used to partition a number into two or more parts, or to help children to partition a number into tens and ones or other place value columns.

In KS2, children can apply their understanding of the part-whole model to add and subtract fractions, decimals and percentages.







Bar Model (single)



Benefits

The single bar model is another type of a part-whole model that can support children in representing calculations to help them unpick the structure.

Cubes and counters can be used in a line as a concrete representation of the bar model.

Discrete bar models are a good starting point with smaller numbers. Each box represents one whole.

The combination bar model can support children to calculate by counting on from the larger number. It is a good stepping stone towards the continuous bar model.

Continuous bar models are useful for a range of values. Each rectangle represents a number. The question mark indicates the value to be found.

In KS2, children can use bar models to represent larger numbers, decimals and fractions.







Bar Model (multiple)

Discrete





7 - 3 = 4

Continuous





Benefits

The multiple bar model is a good way to compare quantities whilst still unpicking the structure.

Two or more bars can be drawn, with a bracket labelling the whole positioned on the right hand side of the bars. Smaller numbers can be represented with a discrete bar model whilst continuous bar models are more effective for larger numbers.

Multiple bar models can also be used to represent the difference in subtraction. An arrow can be used to model the difference.

When working with smaller numbers, children can use cubes and a discrete model to find the difference. This supports children to see how counting on can help when finding the difference.







Number Shapes





Benefits

Number shapes can be useful to support children to subitise numbers as well as explore aggregation, partitioning and number bonds.

When adding numbers, children can see how the parts come together making a whole. As children use number shapes more often, they can start to subitise the total due to their familiarity with the shape of each number.

When subtracting numbers, children can start with the whole and then place one of the parts on top of the whole to see what part is missing. Again, children will start to be able to subitise the part that is missing due to their familiarity with the shapes.

Children can also work systematically to find number bonds. As they increase one number by 1, they can see that the other number decreases by 1 to find all the possible number bonds for a number.







Cubes



Benefits

Cubes can be useful to support children with the addition and subtraction of one-digit numbers.

When adding numbers, children can see how the parts come together to make a whole. Children could use two different colours of cubes to represent the numbers before putting them together to create the whole.

When subtracting numbers, children can start with the whole and then remove the number of cubes that they are subtracting in order to find the answer. This model of subtraction is reduction, or take away.

Cubes can also be useful to look at subtraction as difference. Here, both numbers are made and then lined up to find the difference between the numbers.

Cubes are useful when working with smaller numbers but are less efficient with larger numbers as they are difficult to subitise and children may miscount them.







Ten Frames (within 10)



4 + 3 = 7 4 is a part. 3 + 4 = 7 3 is a part. 7 - 3 = 4 7 is the whole. 7 - 4 = 3



Benefits

When adding and subtracting within 10, the ten frame can support children to understand the different structures of addition and subtraction.

Using the language of parts and wholes represented by objects on the ten frame introduces children to aggregation and partitioning.

Aggregation is a form of addition where parts are combined together to make a whole. Partitioning is a form of subtraction where the whole is split into parts. Using these structures, the ten frame can enable children to find all the number bonds for a number.

Children can also use ten frames to look at augmentation (increasing a number) and take-away (decreasing a number). This can be introduced through a first, then, now structure which shows the change in the number in the 'then' stage. This can be put into a story structure to help children understand the change e.g. First, there were 7 cars. Then, 3 cars left. Now, there are 4 cars.







Ten Frames (within 20)







8 + 7 = 15

5

6 = 8

2

14









Benefits

When adding two single digits, children can make each number on separate ten frames before moving part of one number to make 10 on one of the ten frames. This supports children to see how they have partitioned one of the numbers to make 10, and makes links to effective mental methods of addition.

When subtracting a one-digit number from a two-digit number, firstly make the larger number on 2 ten frames. Remove the smaller number, thinking carefully about how you have partitioned the number to make 10, this supports mental methods of subtraction.

When adding three single-digit numbers, children can make each number on 3 separate 10 frames before considering which order to add the numbers in. They may be able to find a number bond to 10 which makes the calculation easier. Once again, the ten frames support the link to effective mental methods of addition as well as the importance of commutativity.







Bead Strings







Benefits

Different sizes of bead strings can support children at different stages of addition and subtraction.

Bead strings to 10 are very effective at helping children to investigate number bonds up to 10. They can help children to systematically find all the number bonds to 10 by moving one bead at a time to see the different numbers they have partitioned the 10 beads into e.g. 2 + 8 = 10, move one bead, 3 + 7 = 10.

Bead strings to 20 work in a similar way but they also group the beads in fives. Children can apply their knowledge of number bonds to 10 and see the links to number bonds to 20.

Bead strings to 100 are grouped in tens and can support children in number bonds to 100 as well as helping when adding by making ten. Bead strings can show a link to adding to the next 10 on number lines which supports a mental method of addition.







Number Tracks



10 - 4 = 6 1 2 3 4 5 6 7 8 9 10

8	B -	- 7	'=	15	i		(Y	Y	Y	Y	Y	Y	2					
1	2	3	4	5	6	7	8	9	10	11	12	13	14	(15)	16	17	18	19	20

Benefits

Number tracks are useful to support children in their understanding of augmentation and reduction.

When adding, children count on to find the total of the numbers. On a number track, children can place a counter on the starting number and then count on to find the total.

When subtracting, children count back to find their answer. They start at the minuend and then take away the subtrahend to find the difference between the numbers.

Number tracks can work well alongside ten frames and bead strings which can also model counting on or counting back.

Playing board games can help children to become familiar with the idea of counting on using a number track before they move on to number lines.







Number Lines (labelled)



Benefits

Labelled number lines support children in their understanding of addition and subtraction as augmentation and reduction.

Children can start by counting on or back in ones, up or down the number line. This skill links directly to the use of the number track.

Progressing further, children can add numbers by jumping to the nearest 10 and then jumping to the total. This links to the making 10 method which can also be supported by ten frames. The smaller number is partitioned to support children to make a number bond to 10 and to then add on the remaining part.

Children can subtract numbers by firstly jumping to the nearest 10. Again, this can be supported by ten frames so children can see how they partition the smaller number into the two separate jumps.







Number Lines (blank)



Benefits

Blank number lines provide children with a structure to add and subtract numbers in smaller parts.

Developing from labelled number lines, children can add by jumping to the nearest 10 and then adding the rest of the number either as a whole or by adding the tens and ones separately.

Children may also count back on a number line to subtract, again by jumping to the nearest 10 and then subtracting the rest of the number.

Blank number lines can also be used effectively to help children subtract by finding the difference between numbers. This can be done by starting with the smaller number and then counting on to the larger number. They then add up the parts they have counted on to find the difference between the numbers.







Straws





bundle together groups of 10

42 - 17 = 25



Benefits

Straws are an effective way to support children in their understanding of exchange when adding and subtracting 2-digit numbers.

Children can be introduced to the idea of bundling groups of ten when adding smaller numbers and when representing 2-digit numbers. Use elastic bands or other ties to make bundles of ten straws.

When adding numbers, children bundle a group of 10 straws to represent the exchange from 10 ones to 1 ten. They then add the individual straws (ones) and bundles of straws (tens) to find the total.

When subtracting numbers, children unbundle a group of 10 straws to represent the exchange from 1 ten to 10 ones.

Straws provide a good stepping stone to adding and subtracting with Base 10/Dienes.







Base 10/Dienes (addition)



....

Benefits

429

1

Using Base 10 or Dienes is an effective way to support children's understanding of column addition. It is important that children write out their calculations alongside using or drawing Base 10 so they can see the clear links between the written method and the model.

Children should first add without an exchange before moving on to addition with exchange.. The representation becomes less efficient with larger numbers due to the size of Base 10. In this case, place value counters may be the better model to use.

When adding, always start with the smallest place value column. Here are some questions to support children. How many ones are there altogether? Can we make an exchange? (Yes or No) How many do we exchange? (10 ones for 1 ten, show exchanged 10 in tens column by writing 1 in column) How many ones do we have left? (Write in ones column) Repeat for each column.







Base 10/Dienes (subtraction)







Benefits

Using Base 10 or Dienes is an effective way to support children's understanding of column subtraction. It is important that children write out their calculations alongside using or drawing Base 10 so they can see the clear links between the written method and the model.

Children should first subtract without an exchange before moving on to subtraction with exchange. When building the model, children should just make the minuend using Base 10, they then subtract the subtrahend. Highlight this difference to addition to avoid errors by making both numbers. Children start with the smallest place value column. When there are not enough ones/tens/hundreds to subtract in a column, children need to move to the column to the left and exchange e.g. exchange 1 ten for 10 ones. They can then subtract efficiently.

This model is efficient with up to 4-digit numbers. Place value counters are more efficient with larger numbers and decimals.







Place Value Counters (addition)





Benefits

Using place value counters is an effective way to support children's understanding of column addition. It is important that children write out their calculations alongside using or drawing counters so they can see the clear links between the written method and the model.

Children should first add without an exchange before moving on to addition with exchange. Different place value counters can be used to represent larger numbers or decimals. If you don't have place value counters, use normal counters on a place value grid to enable children to experience the exchange between columns.

When adding money, children can also use coins to support their understanding. It is important that children consider how the coins link to the written calculation especially when adding decimal amounts.







Place Value Counters (Subtraction)





Benefits

Using place value counters is an effective way to support children's understanding of column subtraction. It is important that children write out their calculations alongside using or drawing counters so they can see the clear links between the written method and the model.

Children should first subtract without an exchange before moving on to subtraction with exchange. If you don't have place value counters, use normal counters on a place value grid to enable children to experience the exchange between columns.

When building the model, children should just make the minuend using counters, they then subtract the subtrahend. Children start with the smallest place value column. When there are not enough ones/tens/hundreds to subtract in a column, children need to move to the column to the left and exchange e.g. exchange 1 ten for 10 ones. They can then subtract efficiently.







Multiplication and Division







Multiplication- KS1

EYFS	 Have an understanding of number to 10, linking names of numbers, numerals, their value, and their position in the counting order. Subitise (recognise quantities without counting) up to 5. Automatically recall number bonds for numbers 0-5 and <i>for 10</i>, including corresponding partitioning facts. Automatically recall double facts up 5+5 Compare sets of objects up to 10 in different contexts, considering size and difference Explore patterns of numbers within numbers up to 10, including evens and odds. 					
Year	1	2				
Layers of vocabulary Appendix Beck's Tiers of Vocabulary	Basic to subject specific (Beck's Tiers): count in ones, twos tens array, groups of, equal groups odd, even Instructional vocabulary: carry on, continue repeat what comes next? find, choose, collect use, make, build tell me, describe, pick out, talk about, explain, show me, read, write, record	 Basic to subject specific (Beck's Tiers): lots of, groups of ×, times, multiply, multiplied by multiple of once, twice, three times ten times times as (big, long, wide and so on) repeated addition array row, column double, halve share, share equally Instructional vocabulary: carry on, continue, repeat, what comes next? predict describe the pattern describe the rule find, find all, find different, investigate 				















Multiplication- KS2

KS1	Pupils should memorise and reason with numbers in 2, 5 and 10 times They should see ways to represent odd and even numbers and know h Pupils should begin to understand multiplication as scaling in terms of Commutative law shown on array. Repeated addition can be shown mentally on a number line. Inverse relationship between multiplication and division. Use an array	tables. now they are represented in tables. This will help them to understand the pattern in numbers. f double and half (e.g. that tower of cubes is double the height of the other tower). to explore how numbers can be organised into groups.
Year	3	4
Layers of vocabulary Appendix Beck's Tiers of Vocabulary	Basic to subject specific (Beck's Tiers): lots of, groups of ×, times, multiply, multiplication, multiplied by multiple of, product once, twice, three times ten times times as (big, long, wide and so on) repeated addition array row, column double, halve share, share equally one each, two each, three each Instructional vocabulary: carry on, continue repeat what comes next? predict describe the pattern, describe the rule find, find all, find different, investigate choose, decide, collect	 Basic to subject specific (Beck's Tiers): lots of, groups of times, multiply, multiplication, multiplied by multiple of, product once, twice, three times ten times times as (big, long, wide and so on) repeated addition array row, column double, halve, factor, multiple Instructional vocabulary: carry on, continue, repeat what comes next? predict describe the pattern, describe the rule pattern, puzzle, calculate, calculation, mental calculation, method, jotting, answer right, correct, wrong what could we try next? how did you work it out? number sentence sign, operation, symbol, equation
NC 2014	Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including 2 digit numbers times 1 digit numbers progressing to formal written methods.	Multiply 2 digit and 3 digit numbers by a 1 digit number using formal written layout. Solve problems involving multiplying and adding.







Developing	Building tables	Partitioning strategy	Grid method	Building tables	Place value materials	Representing problems
Conceptual/		to double	23 x 8 =		to represent	
Procedural	For example, build	Double 35	20 x 8 =160	For example, build tables	calculations	Multiply a number by itself and then
Understanding	tables using counting		3 x 8 = 24	using counting stick-		make one factor one more and the other
	stick- forwards and	3067 A 500	23 x 8= 184	forwards and backwards	Grid method	one less. What do you notice? Does this
	backwards and with	76	x 20 3	and with missing jumps	(if needed for	always happen?
	missing jumps	Place value materials	8		conceptual	
		to represent	Short	Using known facts	understanding)	Eg 4 x 4 = 16 6 x 6= 36
	Using known facts	calculations	multiplication	If 2 x 3 = 6 then 200 x 3 =		5 x 3 = 15 7 x 5= 35
	If $3 \times 2 = 6$, then $30 \times 2 = 6$		Expanded	600 and 600 ÷3 = 200	346 x 9	Try out more examples to prove your
	2 = 60, 60 ÷3 = 20 and	Partitioning			x 300 40 6	thinking.
	30 = 60 ÷ 2.	Informal recording of	23	Distributivity	9	
		partitioned numbers	<u>x 8</u>	$3 \times (2 + 4) = 3 \times 2 + 3 \times 4$	Short multiplication	A proportion of the second part of the second parts.
	Associativity	15 x 5 = 75	24 (8 x3)	So the '3' can be	Expanded	Tong performance
	$(2 \times 3) \times 4 = 2 \times (3 \times 4)$		<u>160</u> (8 x20)	'distributed' across the		The start years and the part
	6x4-24 (2x12-24	10 x 5 = 50	<u>184</u>	'2 + 4' into 3 times 2 and	346	L
		5 x 5 = 25		3 times 4	<u>x 9</u>	A17 A11 A11 A11 A11
			leading to		54 (9 x 6)	E10 E10 E10 E10
		27 x 3 = 81	compact	3 x (2+4) 3x2 + 3x4	360 (9 x 40)	
			23	leading to	<u>2700</u> (9 x 300)	E12 E04 E90
		20x3 = 60	<u>X 8</u> 194	$13 \times 4 = 10 \times 4 + 3 \times 4 =$	<u>3114</u>	550-0 (689); J.G.M.
		7x3 = 21	$\frac{184}{2}$	52		Place <, >, or = in these number
		20 multiplied by 3			leading to compact	sentences to make them correct
		equals 60 and 7	Representing		346	$50 \times 4 = 4 \times 50$ $4 \times 50 = 40 \times 5$
		multiplied by 3	nrohlems	40 42	<u>x 9</u>	200 x 5 3 x 300
		equals 21. 60 add 21	A group of aliens	40 12	<u>3114</u>	
		Equais of.	live on Planet			
			Xert. Tinions have			
			three legs.			
			Quinions have			
			four legs. The			
			group has 22 legs			







	altogether. How		
	many Tinions and		
	Quinions might		
	there be? Is there		
	more than one		
	solution?		







Division- KS1

EYFS	 Reception: ELG 2020 Have an understanding of number to 10, linking names of numbers, numerals, their value, and their position in the counting order. Subitise (recognise quantities without counting) up to 5. Automatically recall number bonds for numbers 0-5 and <i>for 10</i>, including corresponding partitioning facts. Automatically recall double facts up 5+5 Compare sets of objects up to 10 in different contexts, considering size and difference Explore patterns of numbers within numbers up to 10, including evens and odds. 						
Year	1 2						
Layers of vocabulary Appendix Beck's Tiers of Vocabulary	Basic to subject specific (Beck's Tiers): count in ones, twos tens share, groups of, equal groups odd, even Instructional vocabulary: count out, share out, left, left over	 Basic to subject specific (Beck's Tiers): share, share equally one each, two each, three each group in pairs, threes tens equal groups of ÷, divide, divided by, divided into left, left over Instructional vocabulary: tell me, describe, name, pick out, discuss, talk about, explain, explain your method, explain how you got your answer, give an example of show how you 					
NC 2014	solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher.	Calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication (x), division (÷) and equals (=) signs.					
	Concrete, pictorial, abstract	Concrete, pictorial, abstract					







Procedural Understanding	Using practical contexts and cross- curricular links (PE) such as socks and shoes; animals in the ark to get into groups. Sharing models such as sharing pieces of fruit. Sharing into equal groups 6 frogs shared equally between 2 lily pads gives 3 frogs on each lily pad or Grouping in equal groups 6 frogs grouped in 2s need 3 lily pads to sit on GROUPING ITP How many twos?	rectangular arrangements to show equal groups)	Introduce the \div symbol 15 frogs shared equally between three lily pads 15 \div 3 = 5 or 15 frogs grouped in 5s need 3 lily pads to sit on 15 \div 5 = 3 15 \div 3 = 5 groups of 3 (grouping) 20 \div 2 = 10 0 0 0 0 0 0 0 0	$10 \div 2 = 5$ Repeated addition (to reach a given target) $10 \div 2 = 5$ Repeated addition (to reach a given target) $10 \div 2 = 5$ Repeated addition (to reach a given target) $10 \div 2 = 5$ There are 20 sweets in a bag. How many children can have 5 each? $15 + 5 + 5 + 5 = 5$ Repeated subtraction (from a given quantity) $5 - 5 = 10 = 5$ Links to tables Use language of division linked to tables using counting stick Representing problems Jane has 30 cakes. She wants to share them equally between 5 boxes. How many cakes should go in each box? $30 \div 5 = 6$ Number of cakes in each box = 6
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Division- KS2

KS1	Noticing how counting in multiples if 2, 5 and 10 relates to the number of groups you have counted (introducing times tables) links to division. An understanding of the more you share between, the less each person will get (e.g. would you prefer to share these grapes between 2 people or 3 people? Why?) Secure understanding of grouping means you count the number of groups you have made. Whereas sharing means you count the number of objects in each group.		
Year	3	4	
Layers of vocabulary	 Basic to subject specific (Beck's Tiers): share, share equally one each, two each, three each group in pairs, threes tens equal groups of ÷, divide, division, divided by, divided into left, left over, remainder, dividend, divisor Instructional vocabulary: calculate, work out, solve, investigate question, answer, check 	 Basic to subject specific (Beck's Tiers): share, share equally one each, two each, three each group in pairs, threes tens equal groups of ÷, divide, division, divided by, divided into left, left over, remainder, dividend, divisor Instructional vocabulary: calculate, work out, solve, investigate, question, answer, check 	
NC 2014	Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including 2 digit numbers times 1 digit numbers progressing to formal written methods.	Practise to become fluent in the formal written method of short division with exact answers.	













Year	5	6
Layers of vocabulary Appendix Beck's Tiers of Vocabulary	 Basic to subject specific (Beck's Tiers): equal groups of divide, division, divided by, divided into remainder factor, quotient, divisible by inverse Instructional vocabulary: calculate, work out, solve, investigate question, answer, check same, different missing number/s number facts, number pairs, number bonds greatest value, least value 	 Basic to subject specific (Beck's Tiers): equal groups of divide, division, divided by, divided into remainder factor, quotient, divisible by inverse, remainders as fractions or decimals Instructional vocabulary: calculate, work out, solve, investigate question, answer, check same, different missing number/s number facts, number pairs, number bonds greatest value, least value
NC 2014	Divide numbers up to 4 digits by a 1 digit number using the formal written method of short division and interpret remainders appropriately for the context (as remainders, as fractions, as decimals or by rounding, e.g. $98 \div 4 =$ $= 24 r^2 = 24 \frac{1}{2} = 24.5 \approx 25$). Solve problems involving multiplication and division including using knowledge of factors and multiples, squares and cubes. Solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign. Solve problems involving multiplication and division including scaling by simple fractions and problems involving simple rates.	Divide numbers up to 4 digits by a 2 digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate to the context. Divide numbers up to 4 digits by a 2 digit number using the formal written method of short division where appropriate, interpreting remainders according to the context. Solve problems involving addition, subtraction, multiplication and division.







Developing		Interpreting remainders	Using known facts	
Concontual/	Lising known facts		If $6 \div 2 = 2$ then $6 \div 0.2 = 20$ and	
Dracadural	Using Kilowin facts $f_{1} = 2 + b \circ p = 6000 + 2 = 1$	17 ± 3	$10 \div 2 = 3$ then $0 \div 0.2 = 30$ and $6 \div 0.2 = 30$ and	36 5 9 2 2 4 2
Procedural	$11.6 \div 2 = 3$ then $6000 \div 2 = 2000$ and	what do I know? 17 is not a multiple of 5.	6 ÷ 0.02 = 300	
Understanding	3000 and			
	6000 ÷ 20 = 300			With questions of this type where the
		3 #***	Short division	divisor is close to a number linked to the
	Place value materials to	3. 2	97.6 ÷ 5 =	times tables, encourage the children to
	represent calculations		19.5	use known facts and adjustment to set up
		3 <u>2</u> = 3.4	_2	the partial tables.
	Short division	5	5 9 ⁴ 7.	+
	483 ÷ 7 =	From knowledge of	² 6 ¹ 0	
		decimal/fraction		
	69	equivalents or by	"97.6 divided by 5. 9 tens	
	r1	converting	shared equally between 5 is 1	
	7 4 ⁴ 8 ⁶ 4		with a remainder of 4 tens.	
		· ·	Exchange the ten for 10 units.	
	"484 divided by 7, 4		now have 47 units which shared	
	hundreds cannot be		equally between 5 is 9 with a	
	shared equally between 7	Examples:	remainder of 2 units Exchange	
	so exchange the hundreds	17 EP1 17 -	the 2 units for 20 tenths we	
	for 40 tens 1 now have 48	17 501 + 7 =	now have 26 tenths 26 shared	
	tens which shared equally		equally between 5 equals 5 with	
	botwoon 7 is 6 with a		a remainder of 1 tenth Extend	
	remainder of C tons	$581 \div 7$ could be calculated by the formal written	the dividend with a Q in the	
	Furthering the Citeris.	method of short division or it could be calculated	the dividend with a 0 m the	Representing problems
	Exchange the 6 tens for	hy rearranging the dividend using known facts	nundreaths column. Exchange	Megan divides 500 by 8 and gets the
	60 units, we now have 64	into E60 and 21	the tenth for 10 hundreaths. 10	answer 62r4. She re writes it as $62 \text{ r} 1/2$
	units. 64 shared equally		shared equally between 5	Is she right? Explain your answer
	between 7 equals 9	Benvecenting methods	equals 2. The answer is 19.52."	
	remainder 1. The answer	Connect the connection the coloridation had		
	is 69 r1."	Correct the errors in the calculation below.		Using factors to simplify long division
		Explain the error. $266 \div 5 = /3.1$	Long division	
		7 3 r1	(thinking not generally	25) 815
		5 2 ³ 6 ¹ 6	recorded)	
			384 ÷ 16	







	"What do I know about the divisor?" Record partial tables. 24 16 (38 tens ÷16 = 2 384 r6; 2 x 16 =32) -32 (bring the 4 down) (64 units ÷ 16 =4) 64 - 64 (no remainder) 0	165 5)815 35 5)165 Simplify the fractions for remainders
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Bar Model









Benefits

Children can use the single bar model to represent multiplication as repeated addition. They could use counters, cubes or dots within the bar model to support calculation before moving on to placing digits into the bar model to represent the multiplication.

Division can be represented by showing the total of the bar model and then dividing the bar model into equal groups.

It is important when solving word problems that the bar model represents the problem.

Sometimes, children may look at scaling problems. In this case, more than one bar model is useful to represent this type of problem, e.g. There are 3 girls in a group. There are 5 times more boys than girls. How many boys are there?

The multiple bar model provides an opportunity to compare the groups.







Number Shapes

			5 × 4 =
$\bigcirc \bigcirc$	00	00	4 × 5 =
Contraction of the local division of the loc			

4 X 5 = 20					$5 \times 4 = 20$ $4 \times 5 = 20$
------------	--	--	--	--	--





an - 12 - 12 -

20

20

 $18 \div 3 = 6$

Benefits

Number shapes support children's understanding of multiplication as repeated addition.

Children can build multiplications in a row using the number shapes. When using odd numbers, encourage children to interlock the shapes so there are no gaps in the row. They can then use the tens number shapes along with other necessary shapes over the top of the row to check the total. Using the number shapes in multiplication can support children in discovering patterns of multiplication e.g. odd \times odd = even, odd \times even = odd, even \times even = even.

When dividing, number shapes support children's understanding of division as grouping. Children make the number they are dividing and then place the number shape they are dividing by over the top of the number to find how many groups of the number there are altogether e.g. There are 6 groups of 3 in 18.







Bead Strings



5 × 3 = 15	$15 \div 3 - 5$
$3 \times 5 = 15$	10.0-0



5 × 3 = 15	$15 \div 5 - 3$
$3 \times 5 = 15$	$10 \div 0 = 0$

$$4 \times 5 = 20$$

 $5 \times 4 = 20$ $20 \div 4 = 5$

Benefits

Bead strings to 100 can support children in their understanding of multiplication as repeated addition. Children can build the multiplication using the beads. The colour of beads supports children in seeing how many groups of 10 they have, to calculate the total more efficiently.

Encourage children to count in multiples as they build the number e.g. 4, 8, 12, 16, 20.

Children can also use the bead string to count forwards and backwards in multiples, moving the beads as they count.

When dividing, children build the number they are dividing and then group the beads into the number they are dividing by e.g. 20 divided by 4 – Make 20 and then group the beads into groups of four. Count how many groups you have made to find the answer.







Number Lines (labelled)





 $4 \times 5 = 20$ $5 \times 4 = 20$



 $20 \div 4 = 5$

Benefits

Labelled number lines are useful to support children to count in multiples, forwards and backwards as well as calculating single-digit multiplications.

When multiplying, children start at 0 and then count on to find the product of the numbers.

When dividing, start at the number they are dividing and the count back in jumps of the number they are dividing by until they reach O.

Children record how many jumps they have made to find the answer to the division.

Labelled number lines can be useful with smaller multiples, however they become inefficient as numbers become larger due to the required size of the number line.







Number Lines (blank)



Benefits

Children can use blank number lines to represent scaling as multiplication or division.

Blank number lines with intervals can support children to represent scaling accurately. Children can label intervals with multiples to calculate scaling problems.

Blank number lines without intervals can also be used for children to represent scaling.







Base 10/Dienes (multiplication)



Benefits

Using Base 10 or Dienes is an effective way to support children's understanding of column multiplication. It is important that children write out their calculation alongside the equipment so they can see how the concrete and written representations match.

As numbers become larger in multiplication or the amounts of groups becomes higher, Base 10 / Dienes becomes less efficient due to the amount of equipment and number of exchanges needed.

Base 10 also supports the area model of multiplication well. Children use the equipment to build the number in a rectangular shape which they then find the area of by calculating the total value of the pieces This area model can be linked to the grid method or the formal column method of multiplying 2-digits by 2-digits.







Place Value Counters (multiplication)









Benefits

Using place value counters is an effective way to support children's understanding of column multiplication. It is important that children write out their calculation alongside the equipment so they can see how the concrete and written match.

As numbers become larger in multiplication or the amounts of groups becomes higher, Base 10 / Dienes becomes less efficient due to the amount of equipment and number of exchanges needed The counters should be used to support the understanding of the written method rather than support the arithmetic.

Place value counters also support the area model of multiplication well. Children can see how to multiply 2-digit numbers by 2-digit numbers.







Place Value Counters (division)



Benefits

Using place value counters is an effective way to support children's understanding of division.

When working with smaller numbers, children can use place value counters to share between groups. They start by sharing the larger place value column and work from left to right. If there are any counters left over once they have been shared, they exchange the counter e.g. exchange one ten for ten ones. This method can be linked to the part-whole model to support children to show their thinking.

Place value counters also support children's understanding of short division by grouping the counters rather than sharing them. Children work from left to right through the place value columns and group the counters in the number they are dividing by. If there are any counters left over after they have been grouped, they exchange the counter e.g. exchange one hundred for ten tens.